

DC Machines—Part 3

Losses. Construction.

Electrical Losses

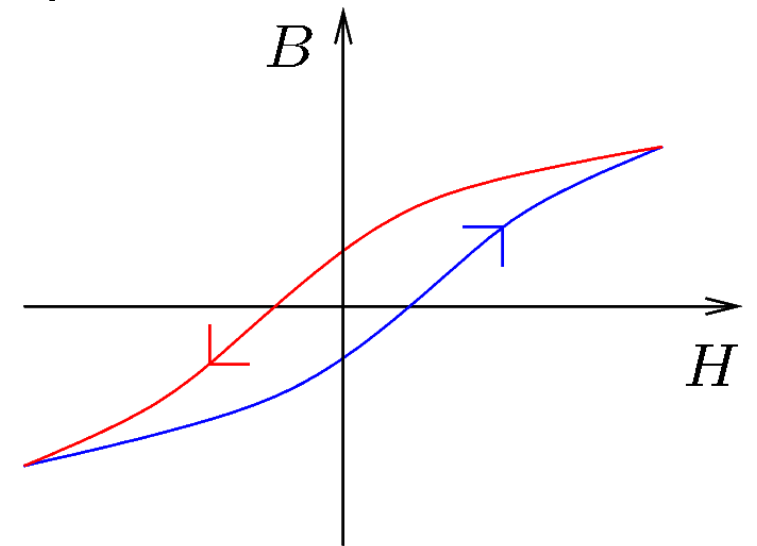
- **Copper losses**: due to the resistance of the windings.
- **Brush contact losses**: the resistance between the brushes and the commutator segments is not zero and not constant.

- Let I_a and I_f be the armature and field currents.
- Let R_a and R_f be the armature and field resistances.
- Copper losses equal to the power dissipated by R_a and R_f :

$$P_c = I_a^2 R_a + I_f^2 R_f$$

Magnetic Losses

- Magnetic losses appear in the core of the coils of the motor.
- They are also known as **iron losses**, because the core is commonly made of steel.
- **Hysteresis** losses appear for core materials in which the dependence of the flux density B on the intensity of the magnetic field H has a hysteresis.
 - When current increases, H increases, and B follows the lower curve.
 - When current decreases, H decreases, and B follows the upper curve.
- Steel has hysteresis, so hysteresis losses are common in motors.
- The lost power is proportional to frequency and the area between the lower and upper curves.
- So there are no losses in constant magnetic field.



Magnetic Losses

- **Eddy current** losses are significant when the core conducts well electricity.
 - A time-varying magnetic field induces currents in the core.
 - Since the resistivity of the core is not zero, power will be dissipated in the core due to the Eddy currents.
- In constant magnetic field there are no Eddy currents, and thus no losses.
- To reduce Eddy currents, cores are made of sheet-steel laminations.
 - Laminations are insulated one from the other.
 - There are Eddy currents in each sheet, but no currents from one sheet to another.

Laminations are coated to prevent currents between laminations.



Other Losses

- Mechanical losses are due to friction.
 - Bearing friction.
 - Brush friction (friction between the brush and the commutator).
 - Windage (friction with the air).
- Stray load: Any other loss not covered before.
 - In the textbook, stray load losses are taken as 1% of the output as a rule of thumb.

Example

A 10 hp 200 V shunt DC motor operates at the rated power. The line current is 48 A, the field resistance is 200 Ω , the armature resistance is 0.5 Ω , the brush contact drop is 2 V, mechanical losses are 400 W, and stray losses 1% of output. Find the efficiency and the core losses. (See problem 4.24 in the textbook for a similar example.)

- The line current is the total current. The input power is $P_{in} = 48 \cdot 200 = 9.6 \text{ kW}$.
- The output power is $P_{out} = 10 \text{ hp} = 7457 \text{ W}$.
- The efficiency is $\eta = \frac{P_{out}}{P_{in}} = 77.68\%$.
- The field current is $I_f = \frac{200 \text{ V}}{200 \Omega} = 1 \text{ A}$.
- The armature current is $I_a = I_L - I_f = 48 - 1 = 47 \text{ A}$.
- The brush contact losses are $P_{bc} = 2 \cdot I_a = 94 \text{ W}$.

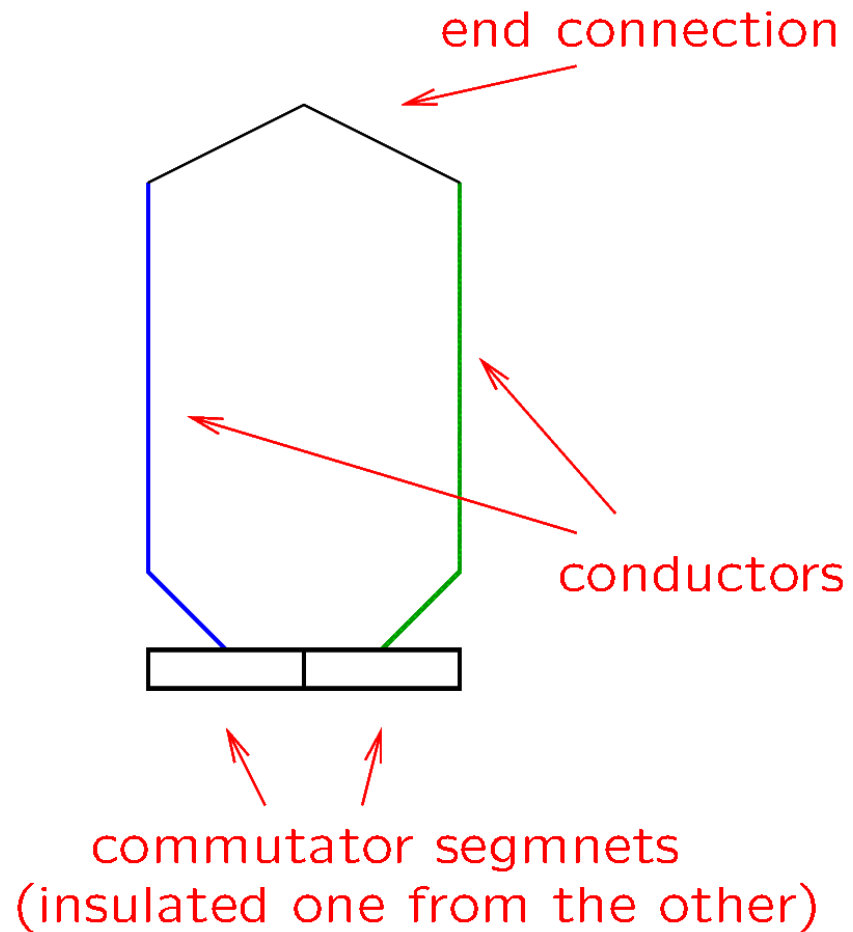
Example (Continued)

- The copper losses are $P_c = I_a^2 R_a + I_f^2 R_f = 47^2 \cdot 0.5 + 1^2 \cdot 200 = 1304.5 \text{ W}$.
- The stray losses are $P_s = 0.01 \cdot P_{out} = 74.57 \text{ W}$.
- The mechanical losses are given: $P_m = 400 \text{ W}$.
- The core losses are the magnetic losses.

$$P_{iron} = P_{in} - P_{out} - P_{bc} - P_c - P_s - P_m = 269.93 \text{ W}.$$

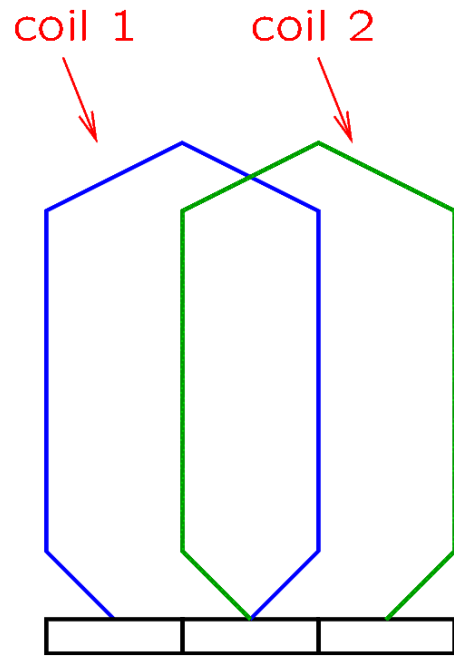
Construction of DC Motors

- The coils of large motors consist of many turns connected in series, where each turn has two conductors.

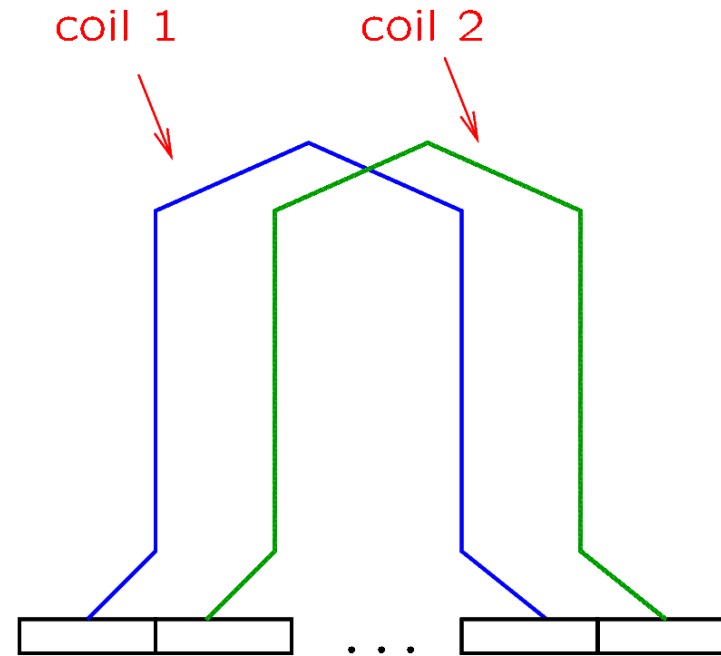


Construction of DC Motors

- There are two types of windings:
 - **Lap windings:** Each armature coil connected to adjacent commutator segments.
 - **Wave windings:** The armature coils are not connected to adjacent segments.



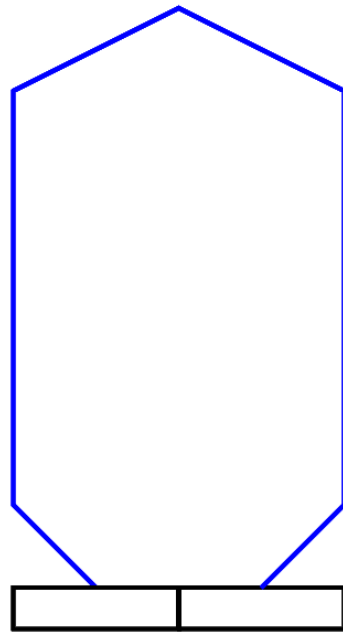
LAP



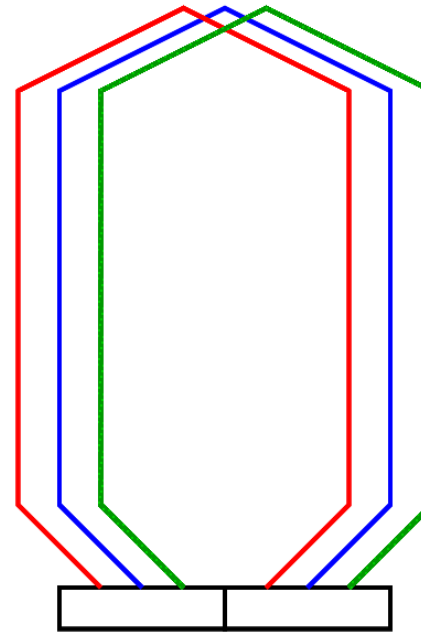
WAVE

Construction of DC Motors

- Windings may be:
 - **Simplex**: no parallel coils.
 - **Multiplex**: several parallel coils.



SIMPLEX



MULTIPLEX

Construction of DC Motors

- Let $PLEX$ be the number of parallel coils.
 - $PLEX = 1$ for simplex windings.
 - $PLEX > 1$ for multiplex windings.
- A machine with wave windings has:
 - $p \geq 2$ stator poles
 - 2 brushes
 - $2 \cdot PLEX$ current paths.
- A machine with lap windings has:
 - $p \geq 2$ stator poles
 - p brushes
 - $p \cdot PLEX$ current paths.

Construction of DC Motors

- Let
 - p be the number of stator poles.
 - z be the total number of conductors.
 - a be the number of current paths.
- The back electromotive force has the equation

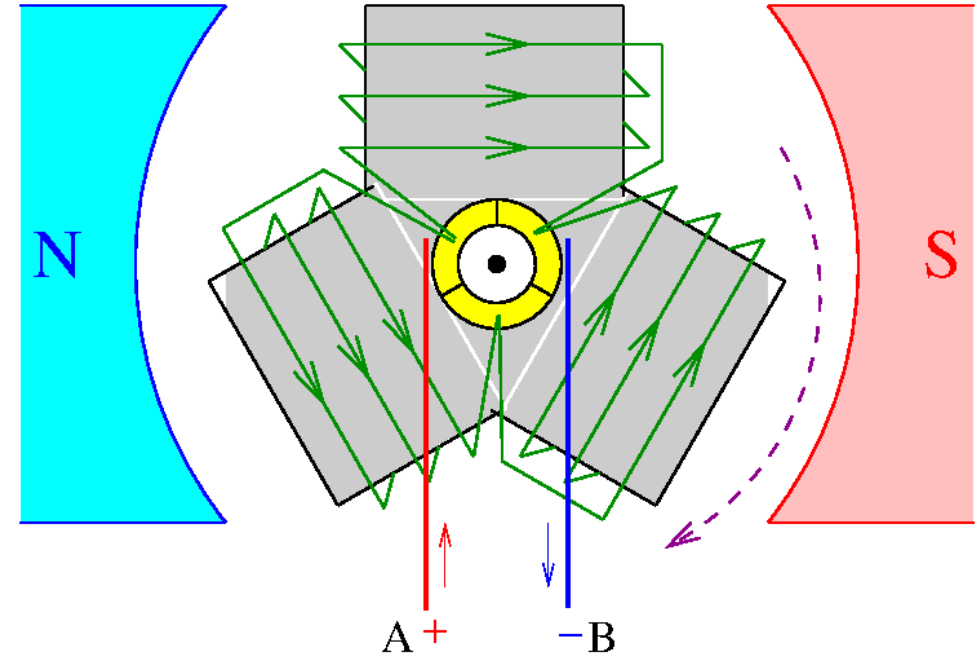
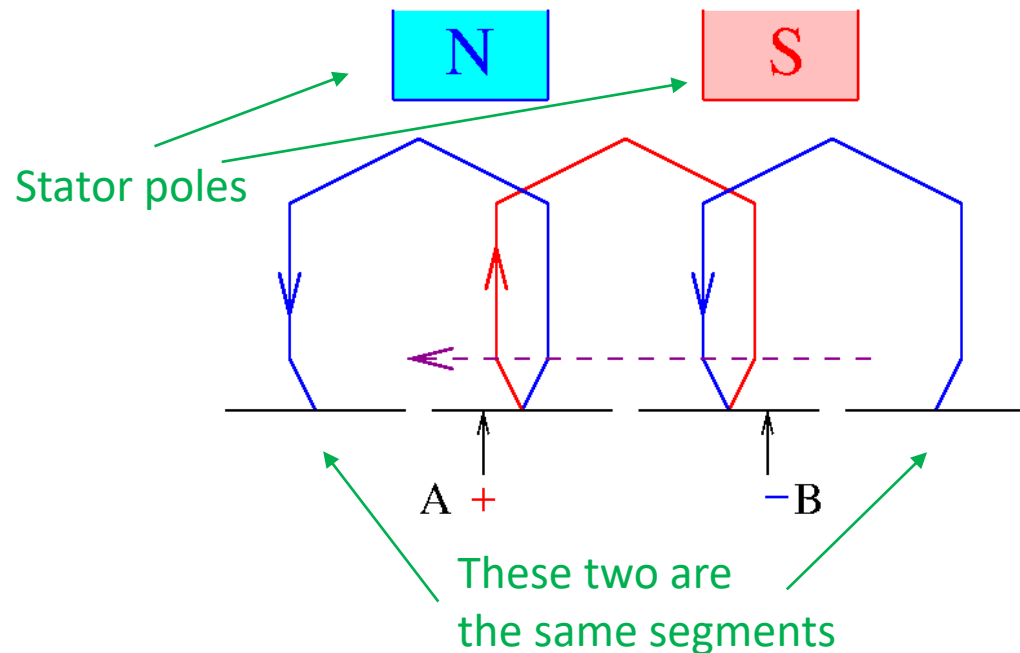
$$E = k_a \Phi \omega$$

where Φ is the flux per pole and

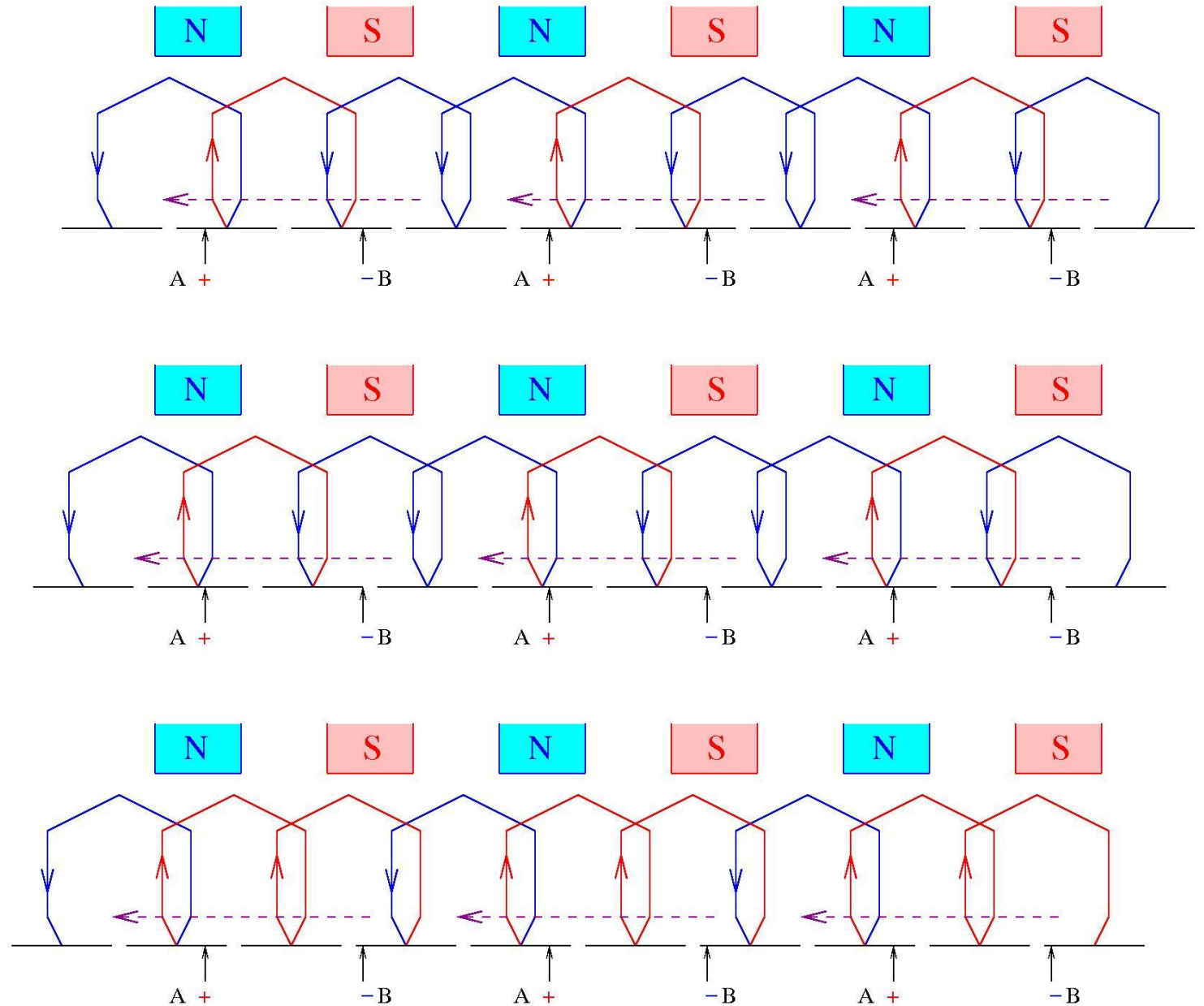
$$k_a = \frac{zp}{2\pi a}$$

Examples

- To describe a motor more easily, it is convenient to “flatten” it and draw it flat.
- A *developed diagram* “is obtained by imagining the armature surface to be removed and then laid out flat” (Quoting from <http://machineryequipmentonline.com/electric-equipment/two-layer-winding-and-multiplex-winding/>, as of April 18, 2020.)
- Below, there are two current paths ($a = 2$) between the two brushes, one shown in red and one in blue.

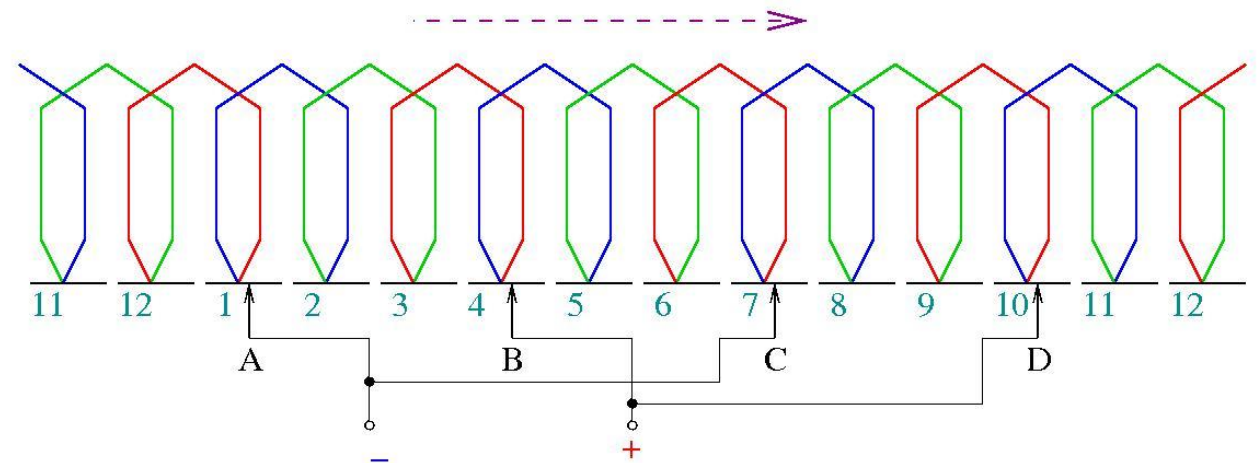
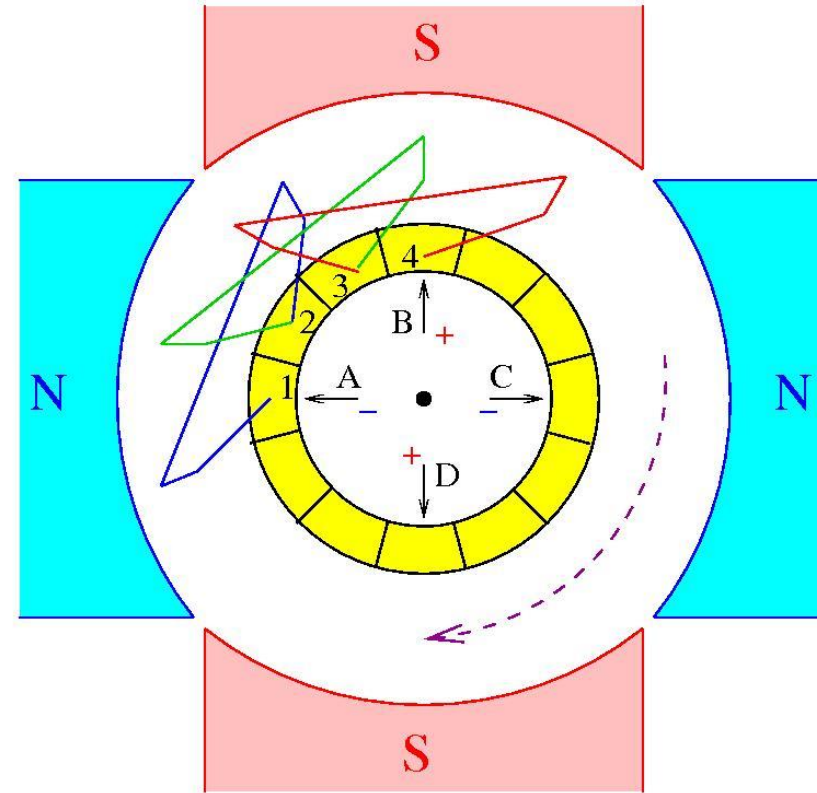


- A red coil has the south polarity and a blue coil the north polarity.
- So a south stator pole repels a red coil and attracts a blue coil.
- The brushes and the stator poles are fixed.
- The armature moves from right to left.
- As it moves, the polarity of the current is switched by the commutator, so that the force is consistently from right to left.



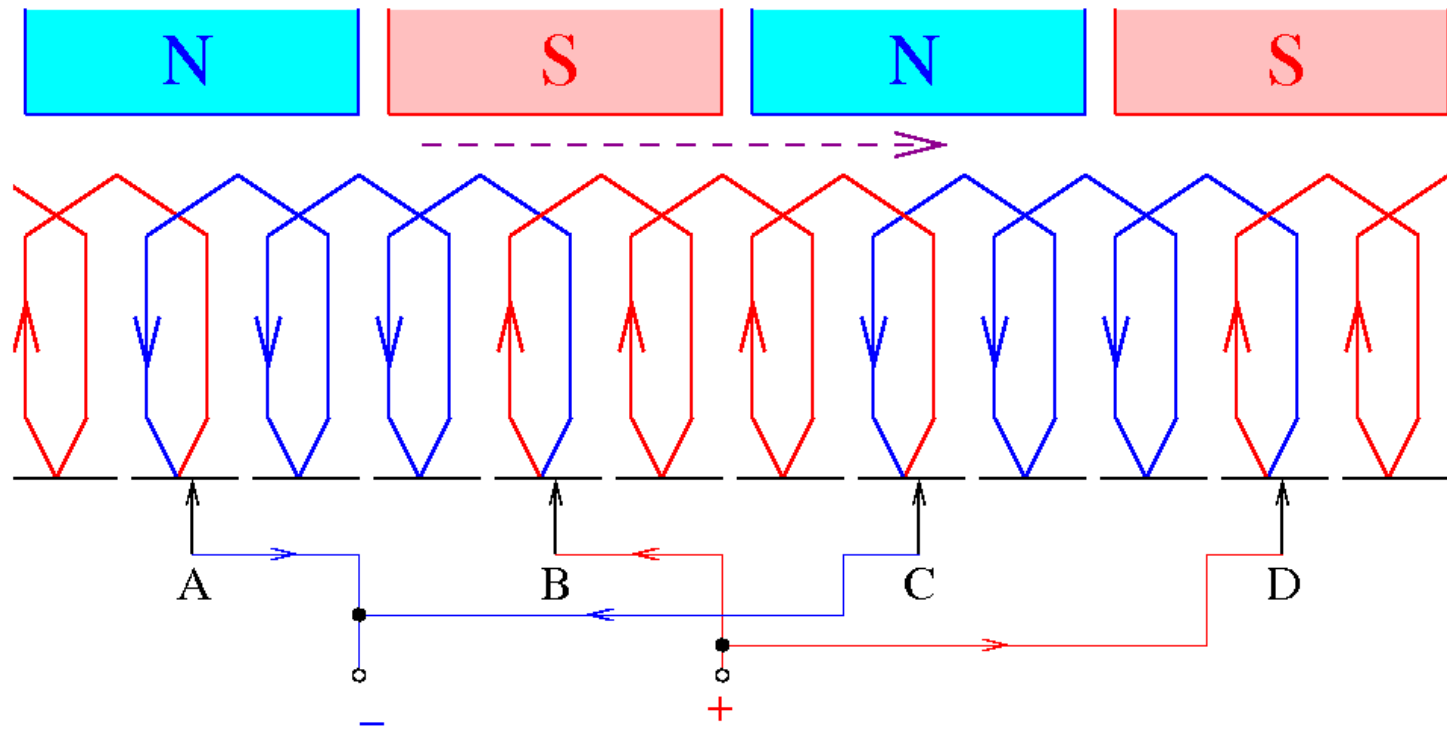
DC Machine with Lap Windings and 4 Stator Poles

- Note that $p = 4$ and $a = 4$.
- There are four current paths:
 - One between brush A and brush B
 - One between brush B and brush C
 - One between brush C and brush D
 - One between brush D and brush A



DC Machine with Lap Windings and 4 Stator Poles

- Note that $p = 4$ and $a = 4$.
- Two current paths marked in red and two marked in blue.



DC Machine with Wave Windings and 4 Stator Poles

- Note that $p = 4$ and $a = 2$.
- There are two current paths between the brushes A and B.
- One path is marked in red and one in blue.

